

# Experimental study on polarimetric-HoloSAR

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**Abstract:** This paper pursues a possibility of fully polarimetric and three-dimensional (3-D) imaging by Holographic Synthetic Aperture Radar Tomography (HoloSAR). HoloSAR is 3-D extension of Circular Synthetic Aperture Radar (CSAR) along the vertical direction whose trajectory is a circle in a horizontal plane. By adding fully polarimetric capability to HoloSAR, it becomes a perfect 3-D imaging radar system which reveals scattering mechanisms from object through scattering power decomposition. This paper attempts to achieve such a prototype system in an anechoic chamber. The experimental result successfully yielded a 3-D image reconstruction of objects with exhibiting polarimetric scattering mechanism.

**Keywords:** Synthetic Aperture Radar (SAR), CSAR, HoloSAR, scattering mechanism

**Classification:** Sensing

## References

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## 1 Introduction

With the advent of Synthetic Aperture Radar (SAR), various functions to SAR systems and data acquisition methods have been applied and added to improve the system performances. Recent SAR advances are well explained in [1], including polarimetry, interferometry, tomography, etc. One goal of SAR applications will be 3-D reconstruction of objects under imaging. Since precise 2-D imaging around  $360^\circ$  is available now by Circular SAR whose trajectory is circular in a horizontal plane, it will be possible to use multiple CSAR in the vertical direction for 3-D imaging.

The pioneering HoloSAR work [2] explains the principle and 3-D reconstruction method in detail together with related problems. This work intends the HoloSAR by adding polarimetric scattering power decomposition scheme [3] to achieve advanced 3-D image reconstruction system. If this kind of Polarimetric-HoloSAR system becomes available, precise 3-D image reconstruction with scattering mechanisms will be available for future applications.

In the following, a brief HoloSAR principle using backprojection method is described in Sect. 2, followed by polarimetric scattering power decomposition scheme in Sect. 3, and the experimental results in Sect. 4. Sect. 5 is the conclusion.

## 2 HoloSAR methodology

Among various CSAR schemes, we use Step Frequency Continuous Wave (SF-CW) radar system [4] for the measurement based on a vector network analyzer.

### 2.1 Formulation

Fig. 1 shows the HoloSAR measurement configuration. The aspect angle  $\varphi$ , and height  $Z_c$  are defined as

$$\varphi = k\Delta\varphi \quad (k = 0, 1, 2, \dots, N_\varphi) \quad (1)$$

$$Z_c = Z_{min} + l\Delta Z_c \quad (l = 0, 1, 2, \dots, N_{Z_c}) \quad (2)$$

where  $\Delta\varphi$  and  $\Delta Z_c$  are sampling intervals,  $N_\varphi$ ,  $N_{Z_c}$  are number of sampling points, and  $Z_{min}$  is the minimum height. Step frequency  $f$  is defined by

$$f = f_0 - \frac{B}{2} + m \frac{B}{N_f} \quad (m = 0, 1, 2, \dots, N_f) \quad (3)$$

where  $f_0$  is the center frequency,  $B$  is bandwidth, and  $N_f$  is number of steps. Transmitted impulse signal  $s$  of SF-CW radar is written as

$$s(t, \omega) = \exp(j\omega t). \quad (4)$$

In the model shown in Fig. 1, the received signal  $p$  for the point target  $(x_n, y_n, z_n)$ .  $p$  is represented by

$$p(t, \omega, \varphi, Z_c) = \sum_{n=1}^{N_{tgt}} g_n \exp\{j\omega[t - \tau_n(\varphi, Z_c)]\} \quad (5)$$

where  $N_{tgt}$  is number of point objects,  $g_n$  is reflection coefficient,  $\tau_n$  is round trip time delay from antenna position to the position  $(x_n, y_n, z_n)$  of object  $n$ . The time delay  $\tau_n$  is represented by

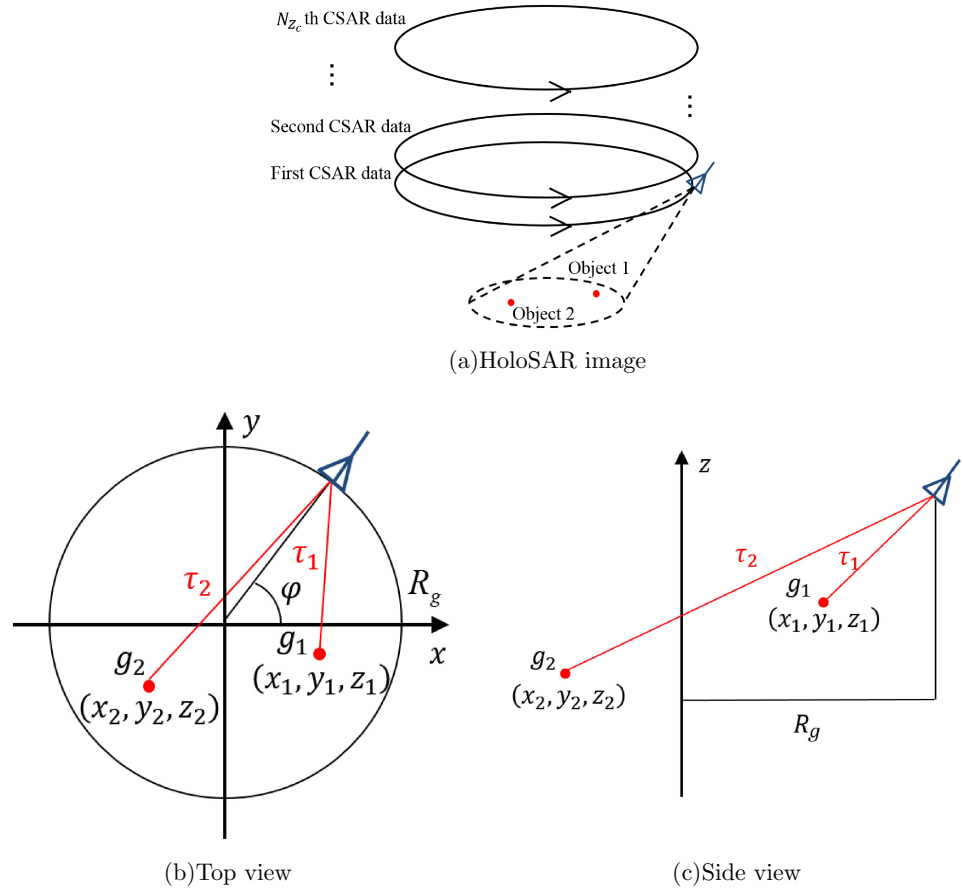


Fig. 1. System model

$$\tau_n(\varphi, Z_c) = \frac{2\sqrt{(x_n - R_g \cos \varphi)^2 + (y_n - R_g \sin \varphi)^2 + (z_n - Z_c)^2}}{c} \quad (6)$$

where  $R_g$  is trajectory radius. The transmission and reception ratio  $S$  becomes

$$S(\omega, \varphi, Z_c) = \frac{p(t, \omega, \varphi, Z_c)}{s(t, \omega, \theta, Z_c)} = \sum_{n=1}^{N_{igt}} g_n \exp\{-j\omega\tau_n(\varphi, Z_c)\}. \quad (7)$$

The HoloSAR reconstruction is achieved by calculating  $g$  in (8) using the back-projection method.  $g$  is represented by

$$g(x, y, z) = \frac{\sum_{k=0}^{N_f} \sum_{l=0}^{N_\varphi} \sum_{m=0}^{N_{Z_c}} S(\omega, \varphi, Z_c) \exp\{j\omega t(x, y, z, \varphi, Z_c)\}}{N_f N_\varphi N_{Z_c}} \quad (8)$$

$$t(x, y, z, \varphi, Z_c) = \frac{2\sqrt{(x - R_g \cos \varphi)^2 + (y - R_g \sin \varphi)^2 + (z - Z_c)^2}}{c} \quad (9)$$

where  $t$  in exponential term is round trip time delay from antenna position to space  $(x, y, z)$ .

## 2.2 Image reconstruction

HoloSAR reconstruction is implemented with the following steps using back-projection scheme.

1. Range compression of raw data

$$S_{(t)} = \mathcal{F}_{(\omega)}[S(\omega, \varphi, Z_c)]^{-1}$$

where,  $\mathcal{F}_{(\omega)}[.]^{-1}$  is fast time inverse Fourier transform.

2. Approximation of round trip time delay from antenna position to space

$$\begin{aligned} t(x, y, z, \varphi, Z_c) &\doteq t'(x_p, y_q, z_r, \varphi, Z_c) \\ &= \frac{2\sqrt{(x_p - R_g \cos \varphi)^2 + (y_q - R_g \sin \varphi)^2 + (z_r - Z_c)^2}}{c} \end{aligned}$$

where,  $x_p, y_q, z_r$  are represented as followed using size of one boxel  $\Delta x \times \Delta y \times \Delta z$ .

$$x_p = x_{min} + p\Delta x \quad (p = 0, 1, 2 \dots N_p)$$

$$y_q = y_{min} + q\Delta x \quad (q = 0, 1, 2 \dots N_q)$$

$$z_r = z_{min} + r\Delta x \quad (r = 0, 1, 2 \dots N_r)$$

where,  $x_{min}, y_{min}, z_{min}$  are minimum analysis area,  $N_p, N_q, N_r$  are number of boxels in each direction.

3. Taking the sum

$$g(x_p, y_q, z_r) = \frac{\sum_{l=0}^{N_\varphi} \sum_{m=0}^{N_{Z_c}} S_{(t)}(\omega, \varphi, Z_c) \exp\{j\omega t'(x_p, y_q, z_r, \varphi, Z_c)\}}{N_\varphi N_{Z_c}}.$$

### 3 Polarimetric scattering power decomposition

By the polarimetric measurement using the combination of Tx and Rx with H-pol. and V-pol. basis, it is possible to obtain scattering matrix. This matrix can be transferred to Pauli vector,

$$\mathbf{k}_P = \frac{1}{\sqrt{2}} \begin{bmatrix} O_{HH} + O_{VV} \\ O_{HH} - O_{VV} \\ 2O_{HV} \end{bmatrix} \quad (10)$$

where  $O_{HH}, O_{HV}, O_{VH}, O_{VV}$  are observed scattering matrix elements after the reconstruction processing. The Pauli vector is used to create coherency matrix which retain the second order statistics of polarimetric information. The ensemble average of the coherency matrix, denoted as  $\langle [T] \rangle$ , is defined by,

$$\langle [T] \rangle = \frac{1}{N_{ave}} \sum \mathbf{k}_P \mathbf{k}_P^\dagger = \begin{bmatrix} T_{11} & T_{12} & T_{13} \\ T_{21} & T_{22} & T_{23} \\ T_{31} & T_{32} & T_{33} \end{bmatrix} \quad (11)$$

where  $\dagger$  is complex conjugate and transpose, and  $N_{ave}$  is the number of averaged boxels. The scattering power decomposition method expand the measured coherency matrix into sub-matrices representing scattering models [5], as follows:

$$\langle [T] \rangle = f_s[T]_{surface} + f_d[T]_{double} + f_v[T]_{volume} + f_c[T]_{helix}. \quad (12)$$

By comparing the quantity of the measured data and scattering model, we can retrieve the following 4-scattering powers to be used in the next section.

The surface scattering power  $P_s$  (Blue color assigned)

The double bounce power  $P_d$  (Red)

The volume scattering power  $P_v$  (Green)

The helix scattering power  $P_c$  (Yellow)

## 4 Experimental results

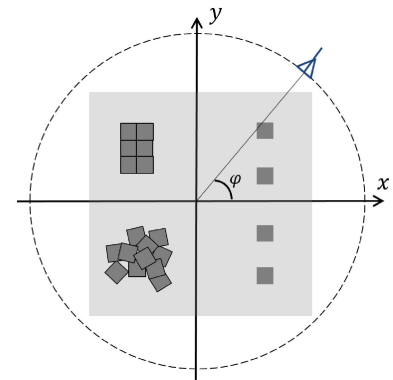
In this section, we pursue a possibility of Polarimetric-HoloSAR to retrieve scattering mechanism from reconstructed images of concrete blocks in an echoic chamber measurement.

### 4.1 Measurement specification

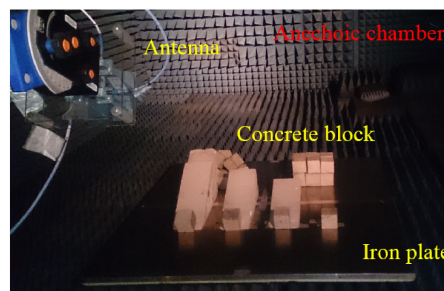
Measurement specifications and object configuration are shown in Fig. 2. We used several concrete blocks with cube of 0.1 m, placed on an iron plate. The combination of these blocks were modeled as a building, collapsed building, and four isolated houses as shown in Fig. 2(b) for top view. Fig. 2(c) is a photo taken from  $\varphi = 0^\circ$ , along the x axis of Fig. 2(b). Fig. 2(d) is a model of collapsed building whose maximum height is 0.3 m. Elevation angle of four isolated houses are  $0^\circ$ ,  $10^\circ$ ,  $20^\circ$ ,  $30^\circ$  from the top of Fig. 2(b) with respect to x-axis. The origin of antenna height is set on the iron plate surface at  $z = 0$ . At each height, we used Inverse SAR (ISAR) scheme [6] to obtain fully polarimetric data set in a horizontal plane with circular trajectory.

Center frequency	15 GHz
Bandwidth	4 GHz
Number of steps	401 steps
Off-nadir angle	$60^\circ$
Trajectory radius	2.25 m
Height interval	0.02 m
Antenna height	0.8~1.8 m
Aspect angle interval	$0.2^\circ$

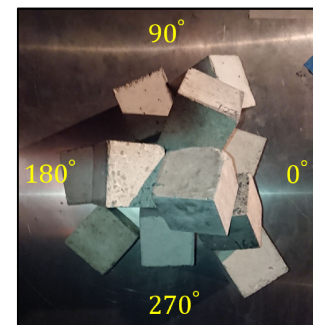
(a) Radar parameters



(b) Top view installation



(c) Photo seen from the x-axis



(d) collapsed building model

Fig. 2. Experimental situation

## 4.2 3-D image reconstruction

The data sets of fully polarimetric data by HoloSAR measurement were used to create 3-D image using the following parameters,

Size of one boxel:  $\Delta x \times \Delta y \times \Delta z = 0.01 \times 0.01 \times 0.01$  [m]

Analysis area:  $-1 \leq x \leq 1, -1 \leq y \leq 1, -0.5 \leq z \leq 0.5$  [m]

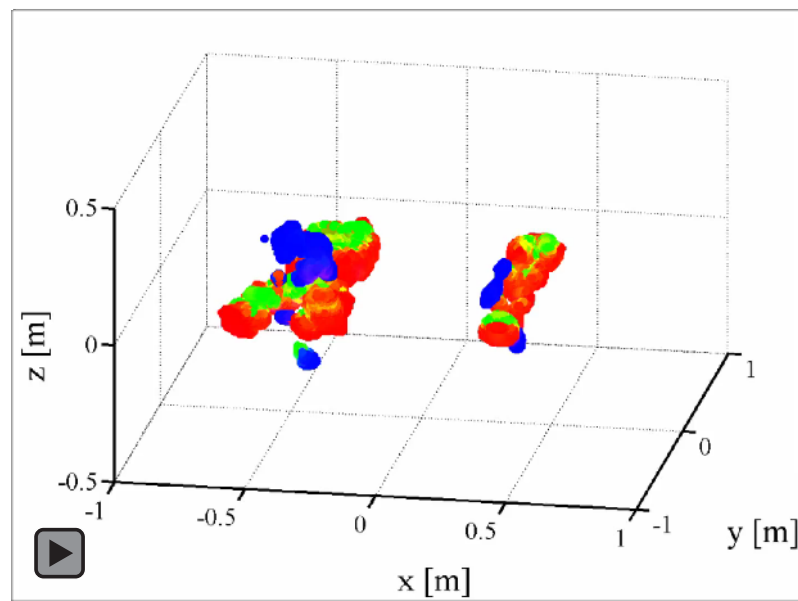
Averaging size:  $x \times y \times z = 3 \times 3 \times 3$  [boxel]

Threshold: maximum power [dB]  $-20$  [dB]

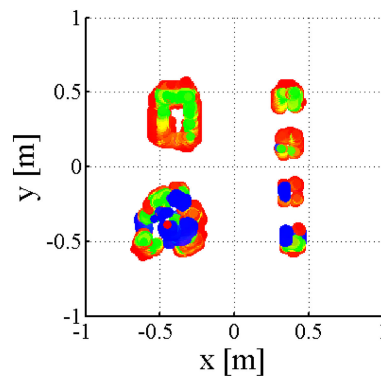
Fig. 3 shows a 3-D and fully polarimetric scattering power image of the scene under test (Fig. 2). The movie file Fig. 3(a) shows the reconstructed image viewed from 360° directions. Fig. 3(b) shows the image seen from top, while (c) is side view image (seen at  $\varphi = 0^\circ$ ).

As can be seen in Fig. 3, the image shows accurate mapping in the horizontal plane. The plotted box position is corresponding to the actual position in the measurement situation. The accurate 2-D positioning is the most advantageous of multi-lateral observations of HoloSAR.

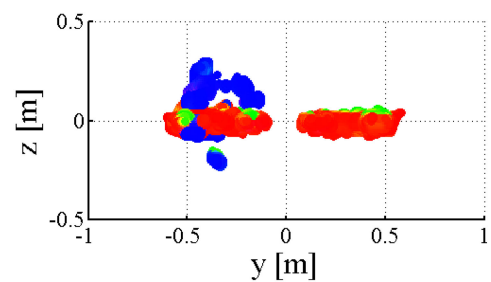
The second advantage is an estimation of the maximum object height by vertical information of HoloSAR measurement. Also in the block with elevation



(a) Movie file seen from 360° directions



(b) Top view



(c) Side view

Fig. 3. Polarimetric reconstruction image of Fig. 2.

angles of  $20^\circ$  and  $30^\circ$ , strong surface scattering  $P_s$  is seen. Since the elevation angle of a typical houses are  $15^\circ$  to  $30^\circ$ , the house height can be detected.

These above two advantages may be common to HoloSAR systems. The most important and third advantage of Polarimetric-HoloSAR is correct building detection capability by strong scattering power  $P_d$  caused by the double bounce scattering mechanism. By circular trajectory observation, it is possible to receive very strong double bounce scattering generated by the right angle structure of building walls and the ground. This happens four times if the building is rectangular. By adding the polarimetric capability, it becomes possible to classify or identify objects more accurately.

## 5 Conclusion

In this paper, we examined the possibility of fully polarimetric and HoloSAR to retrieve 3-D scattering information from objects under imaging scene. Basic experimental results showed advantages of HoloSAR for 1) accurate 2-D positioning in the horizontal plane, and 2) height information in the vertical direction. Furthermore, by polarimetric measurement, the capability of scattering mechanism information retrieval is added to the HoloSAR system, which leads to classify or identify objects accurately. If this kind of polarimetric HoloSAR systems becomes available, precise 3-D image reconstruction will be available for future applications.