# $\mathrm{He} *\left(\mathbf{2}^{3} \mathrm{~S}\right)$ Penning ionization of $\mathrm{H}_{2} \mathrm{~S}$. I. Theoretical Franck-Condon factors for the $\mathrm{H}_{2} \mathrm{~S}\left(\tilde{\boldsymbol{X}}^{1} A_{1}, v^{\prime}=0\right) \rightarrow \mathrm{H}_{2} \mathbf{S}^{+}\left(\tilde{X}^{2} B_{1}, \tilde{A}^{2} A_{1}\right)$ ionization and $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{\boldsymbol{A}}-\tilde{\boldsymbol{X}})$ transition 

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#### Abstract

In order to elucidate the ionization dynamics, in particular the vibrational distribution, of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ produced by the Penning ionization of $\mathrm{H}_{2} \mathrm{~S}$ with $\mathrm{He}^{*}\left(2^{3} S\right)$ atoms, the Franck-Condon factors (FCFs) were presented for the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ ionization and the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ transition, and Einstein's $A$ coefficients were presented for the latter transition. The FCFs were obtained by quantum vibrational calculations using the global potential energy surfaces (PESs) of $\mathrm{H}_{2} \mathrm{~S}\left(\widetilde{X}^{1} A_{1}\right)$ and $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{X}^{2} B_{1}, \widetilde{A}^{2} A_{1}, \widetilde{B}^{2} B_{2}\right)$ electronic states. The global PESs were determined by the multireference configuration interaction calculations with the Davidson correction and the interpolant moving least squares method combined with the Shepard interpolation. The obtained FCFs exhibit that the $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X})$ state primarily populates the vibrational ground state since its equilibrium geometry is almost equal to that of $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$, while the bending mode ( $\nu_{2}$ ) is strongly enhanced for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ state; the maximum in the population is around $\nu_{2}=6-7$. In the same manner, the bending progressions are expected to consist of the great part of the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ emission. A detailed comparison with the experimental study for this system is reported in the accompanying paper, Paper II. © 2003 American Institute of Physics. [DOI: 10.1063/1.1602063]


## I. INTRODUCTION

In the Penning ionization of $\mathrm{He}^{*}\left(2^{3} S\right)$ with hydrogen sulfide, the $\widetilde{X}^{2} B_{1}, \widetilde{A}^{2} A_{1}$, and $\widetilde{B}^{2} B_{1}$ states of the $\mathrm{H}_{2} \mathrm{~S}^{+}$ion were observed by electron spectroscopy. ${ }^{1-3}$ In contrast, no emission from the parent ion was identified by Penning ionization optical spectroscopy. ${ }^{4,5}$ Most recently we have assigned the $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{A}^{2} A_{1}-\widetilde{X}^{2} B_{1}\right)$ emission produced by the collision of $\mathrm{H}_{2} \mathrm{~S}$ with the $\mathrm{He}^{*}\left(2^{3} S\right)$ atom and have analyzed the vibrational and rotational populations of the $\widetilde{A}^{2} A_{1}$ state; the details are reported in Paper II. The analysis to elucidate the vibrational populations of the $\widetilde{A}$ state requires several types of spectroscopic data such as vibrational and rotational energies, transition probabilities, Franck-Condon factors (FCFs), and Hönl-London factors. Several groups have carried out theoretical calculations for $\mathrm{H}_{2} \mathrm{~S}^{+}$and iso-electronic species. ${ }^{6-8}$ Unfortunately, the published data regarding vibrational energies and FCFs have been found to be inadequate from both experimental and theoretical standpoints for analyzing the observed spectra in our preliminary analysis. Bruna et al. ${ }^{8}$ have calculated FCFs for the symmetric and antisymmetric stretching and bending modes in the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ transition by a one-dimension model. Never-

[^0]theless, the vibrational states of the $\widetilde{X}$ and $\widetilde{A}$ states were found to show large anharmonic characters. We therefore obtained these data by a three-dimensional calculation in the present study.

The topography of the potential energy surface (PES) is the key to understanding Penning ionization processes since a chemical reaction is described by nuclear motion on a PES. Three-dimensional PESs of both the target $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ molecule and the product $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ ions were obtained by an $a b$ initio molecular orbital (MO) configuration interaction (CI) method, and three-dimensional transition moments were obtained for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{A}-\widetilde{X})$ system. Furthermore, we carried out quantum vibrational calculations on these potential surfaces to obtain the vibrational eigenvalues and eigenfunctions and obtained the FCFs for the $\mathrm{H}_{2} \mathrm{~S}(\tilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X}, \tilde{A})$ ionization and the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ transition.

The present paper outlines first the $a b$ initio MO CI calculations used in our determination of the PESs, as well as quantum vibrational calculations. Subsequently, we describe the potential energy surfaces for the $\widetilde{X}^{2} B_{1}, \widetilde{A}^{2} A_{1}$, and $\widetilde{B}^{2} B_{1}$ states of $\mathrm{H}_{2} \mathrm{~S}^{+}$and the ground state of $\mathrm{H}_{2} \mathrm{~S}$, and also vibrational states for each electronic state. Finally, the obtained FCFs and Einstein's $A$ coefficients are summarized and discussed in comparison with the other results. The mechanism of the Penning ionization for the $\mathrm{He}^{*}\left(2^{3} S\right)$ $+\mathrm{H}_{2} \mathrm{~S}$ reaction are discussed in Paper II.

## II. THEORETICAL CALCULATIONS

## A. Ab initio MO Cl calculations

Determination of the global PES is quite important to calculations of the higher vibrational states, as it is necessary to take into account the anharmonicity of the PES, especially for the electronic excited states. In other words, most electronic excited states do not possess a single minimum such as the electronic ground state. Therefore, we performed $a b$ initio calculations for approximately 4000 molecular conformations on each three-dimensional PES, even for the electronic excited states.

The basis set used in the present work was the diffuse function augmented, correlation consistent, polarized valence, triple zeta (aug-cc-pVTZ) of Woon and Dunning. ${ }^{9}$ The MOs were determined by complete active space selfconsistent (CASSCF) calculations. After determining the MOs, multireference configuration interaction (MRCI) calculations were carried out.
$\mathrm{H}_{2} \mathrm{~S}$ is an 18 -electron system, and the electronic configuration of the ground state for the valence is

$$
\left(4 a_{1}\right)^{2}\left(2 b_{2}\right)^{2}\left(5 a_{1}\right)^{2}\left(2 b_{1}\right)^{2}
$$

The symmetric species of $\mathrm{H}_{2} \mathrm{~S}\left(\widetilde{X}^{1} A_{1}\right)$ is ${ }^{1} A^{\prime}$. The three lowest $\mathrm{H}_{2} \mathrm{~S}^{+}$ion states come out of the three highest occupied orbitals, as follows:

$$
\begin{aligned}
& \widetilde{X}^{2} B_{1}:\left(2 b_{2}\right)^{2}\left(5 a_{1}\right)^{2}\left(2 b_{1}\right)^{1}, \\
& \widetilde{A}^{2} A_{1}:\left(2 b_{2}\right)^{2}\left(5 a_{1}\right)^{1}\left(2 b_{1}\right)^{2}, \\
& \widetilde{B}^{2} B_{2}:\left(2 b_{2}\right)^{1}\left(5 a_{1}\right)^{2}\left(2 b_{1}\right)^{2} .
\end{aligned}
$$

The two lowest $\tilde{X}$ and $\tilde{A}$ states are derived from ${ }^{2} \Pi_{u}$ from the Renner-Teller interaction, and the three states correlate with the $\mathrm{H}_{2}\left(X^{1} \Sigma^{+}\right)+\mathrm{S}^{+}\left({ }^{2} D_{u}\right)$ system in the dissociation limit. To obtain the MOs necessary to describe these electronic states, the state-averaged CASSCF calculations were carried out with inclusion of a full valence as the active space orbitals. The active space of the MRCI calculations is the same as that of CASSCF, and the configuration state functions were generated by single and double excitations with respect to the reference configurations used in the CASSCF calculation, except for the frozen-core orbitals, $1 s$, $2 s$, and $2 p(\mathrm{~S})$. Moreover, the Davidson correction for the MRCI calculation was employed to include the correlation energy due to higher excitations. ${ }^{10-12}$ The total number of configurations for the final internally contracted MRCI calculations is approximately 150000 for the $A^{\prime}$ symmetry. ${ }^{13,14}$ In the present work, the potential energies for the electronic ground state, $1^{1} A^{\prime}$, of $\mathrm{H}_{2} \mathrm{~S}$, and the electronic ground state, $1^{2} A^{\prime}$, and the next two electronic excited states, $2^{2} A^{\prime}$ and $1^{2} A^{\prime \prime}$, of $\mathrm{H}_{2} \mathrm{~S}^{+}$were finally obtained in the $C_{s}$ symmetry. All calculations were carried out with the MOLPRO program package. ${ }^{15}$ The computer was an SGI Origin 2800 owned by the Research Center for Computational Science at Okazaki.

Potential energies for $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{H}_{2} \mathrm{~S}^{+}$were calculated at 3600 and 4700 geometries, respectively, and were interpolated by the interpolant moving least squares method combined with the Shepard method ${ }^{16-18}$ to carry out a quantum


FIG. 1. Jacobi coordinates, bond length-bond angle coordinates, and Cartesian $(x-y)$ coordinates.
vibrational calculation on the PESs. The parameters to determine the weight functions [see Eq. (6) of Ref. 16] were chosen to be $a=0.03$ and $p=3$.

## B. Quantum vibrational calculations

Since some of the highly vibrational excited states could be characterized with the unlocalized wave function that does not look like the zero-point vibrational wave function, we performed a quantum vibrational calculation based on the discrete variable representations. ${ }^{19-22}$ The body-fixed Jacobi coordinates, which are shown in Fig. 1, were employed to describe the relative positions of the three nuclei in the body fixed plane; $R$ is the distance between the $S$ atom and the center of mass of two H atoms, $r$ is the distance between the two H atoms, and the $\theta$ is the angle between the vectors $R$ and $r$. ${ }^{23}$ The Hamiltonian matrix and associated wave functions are represented with evenly spaced grids in $R$ and $r$, and associated Legendre polynominals to describe $\cos \theta$. The grid parameters were suitable for the radial part: $\left(N_{R}=95, R_{\text {min }}\right.$

TABLE I. Equilibrium geometries of $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{H}_{2} \mathrm{~S}^{+}$.

| State | Parameter ${ }^{\text {a }}$ | This work | MRD-CI ${ }^{\text {b }}$ | Experiment |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{~S}\left(\widetilde{X}^{1} A_{1}\right)$ | $r_{\text {SH }}$ | 1.342 | $\cdots$ | $1.328^{\text {c }}$ |
|  | $\alpha$ | 92.4 | . | $92.2^{\text {c }}$ |
| $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{X}^{2} B_{1}\right)$ | $r_{\text {SH }}$ | 1.362 | 1.364 | $1.358^{\text {de }}$ |
|  | $\alpha$ | 93.0 | 92.7 | $92.5{ }^{\text {d }} 92.9{ }^{\text {e }}$ |
|  | $\Delta E_{e} / \mathrm{eV}$ | 10.34 | 10.17 | $\begin{aligned} & 10.48,{ }^{\mathrm{f}} 10.43,{ }^{\mathrm{g}} 10.47,{ }^{\mathrm{h}} \\ & 10.466^{\mathrm{i}} \end{aligned}$ |
| $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{A}^{2} A_{1}\right)$ | $r_{\text {SH }}$ | 1.362 | 1.366 | $1.376,{ }^{\text {d }} 1.369^{\text {e }}$ |
|  | $\alpha$ | 126.8 | 128.3 | $128,{ }^{\text {d }} 127^{\text {e }}$ |
|  | $\Delta E_{e} / \mathrm{eV}$ | 12.63 | 13.16 | $\begin{aligned} & 12.76,{ }^{\mathrm{f}} 12.81,{ }^{\mathrm{g}} 12.78,{ }^{\mathrm{h}} \\ & 12.777^{\mathrm{i}} \end{aligned}$ |
| $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{B}^{2} B_{2}\right)$ | $r_{\text {SH }}$ | 1.550 | 1.593 | ... |
|  | $\alpha$ | 33.8 | 32.2 | $\cdots$ |
|  | $\Delta E_{e} / \mathrm{eV}$ | 13.42 | 15.46 | $\begin{aligned} & 14.56,{ }^{\mathrm{f}} 14.79,{ }^{\mathrm{g}} 14.78,{ }^{\mathrm{h}} \\ & 14.643^{\mathrm{i}} \end{aligned}$ |

[^1]$\left.=0.0 a_{0}, R_{\max }=7.0 a_{0}\right) \quad$ and $\quad\left(N_{r}=95, r_{\min }=0.0 a_{0}, r_{\max }\right.$ $=7.0 a_{0}$ ), where $N$ is the number of grid points and $a_{0}$ is the Bohr radius. The number of Legendre functions was 50 for the angular part. The method adopted for the diagonalization of the Hamiltonian matrix is the implicitly restricted Lanczos method. ${ }^{24}$ In the present work, assuming the total angular momentum $J=0$, the lowest 100 vibrational states were obtained for the $A^{\prime}\left({ }^{1} A_{1}\right)$ state of $\mathrm{H}_{2} \mathrm{~S}$. Those for the $A^{\prime}\left({ }^{2} A_{1}\right)$ and $A^{\prime \prime}\left({ }^{2} B_{1}\right)$ states of $\mathrm{H}_{2} \mathrm{~S}^{+}$were calculated up to the 200 states, and the FCFs were then evaluated as the square of the overlap integrals between the initial and final states. The electronic transition probabilities for spontaneous emission ${ }^{25}$ were also evaluated for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ transition as the square of the transition moments that depend on both the initial and final vibrational states.

## III. RESULTS AND DISCUSSION

## A. Potential energy surfaces

The equilibrium geometry of each state was calculated via polynomial fit for the potential energy data. Table I summarizes the geometries thus determined compared with the published data. Our theoretical results agree well with the experimental data. Figure 2 shows the potential surfaces of $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$, where $r$ is fixed at the equilibrium for each state. The energy zero of each electronic state is taken to be at the global energy minimum of the corresponding state; $\widetilde{X}^{1} A_{1}$ of $\mathrm{H}_{2} \mathrm{~S}$, and $\widetilde{X}^{2} B_{1}, \widetilde{A}^{2} A_{1}$, and


FIG. 2. Potential energy surfaces for (a) $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$, (b) $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X})$, and (c) $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$; the $r$ is fixed at the equilibrium distance for each state. The asterisk $\left(^{*}\right)$ represents the potential minimum. The numerical values represent the energy differences from each potential minimum in eV . Narrow and thick contours are shown in the interval of 0.2 and 2.0 eV , respectively.


FIG. 3. Potential curves of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A}, \widetilde{B})$ for $\alpha ; r_{\text {SH }}$ is fixed at the equilibrium length of $1.342 \AA$ for $\mathrm{H}_{2} \mathrm{~S}(\tilde{X})$. The circles show the calculated values. The potential energy, $V$, means the difference from the minimum for the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ state. The vertical line near $92^{\circ}$ represents the equilibrium angle for $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$.
$\widetilde{B}^{2} B_{2}$ of $\mathrm{H}_{2} \mathrm{~S}^{+}$are $-398.94067677,-398.56085883$, -398.47665307 , and $-398.44747283 E_{h}$, respectively. As shown in Fig. 2, both of the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X})$ states have the similar topographical feature, indicating that the $0-0$ transition should be a dominant process between these states.

Figure 3 shows the potential energy curves for the three lowest states in $\mathrm{H}_{2} \mathrm{~S}^{+}$, where $r_{\mathrm{SH}}$ is fixed at $1.342 \AA$, which is the equilibrium length for $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$. It is clearly seen that there is a Renner-Teller pair of the $\widetilde{A}^{2} A_{1}$ and $\widetilde{X}^{2} B_{1}$ states at around the linear conformation. Although the $\widetilde{A}^{2} A_{1}$ and $\widetilde{B}^{2} B_{2}$ states cross each other at around $\alpha=70^{\circ}$, these states avoid crossing due to the same symmetry $A^{\prime}$ because the molecular symmetry comes to the lowest symmetry $\left(C_{s}\right)$. Thus, the vibrational states of the $\widetilde{A}^{2} A_{1}$ and $\widetilde{B}^{2} B_{2}$ states can be mixed due to the nonadiabatic transitions. Furthermore,


FIG. 4. Electronic transition moments for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ system vs $\alpha$ at $\theta=90^{\circ}$ and $r=1.9 \AA$ (circle) and $r=2.4 \AA$ (square).

TABLE II. Vibrational energies, $G$, calculated for $\mathrm{H}_{2} \mathrm{~S}\left(\widetilde{X}^{1} A_{1}\right)$ and $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{X}^{2} B_{1}, \widetilde{A}^{2} A_{1}\right)$ and their assignments. ${ }^{\text {a }}$

| $\mathrm{H}_{2} \mathrm{~S}\left(\widetilde{X}^{1} A_{1}\right)$ |  | $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{X}^{2} B_{1}\right)$ |  | $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{A}^{2} A_{1}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ( $G / \mathrm{cm}^{-1}$ ) | $\left(\nu_{1}, \nu_{2}, \nu_{3}\right)$ | $\left(G / \mathrm{cm}^{-1}\right)$ | $\left(\nu_{1}, \nu_{2}, \nu_{3}\right)$ | $\left(G / \mathrm{cm}^{-1}\right)$ | $\left(\nu_{1}, \nu_{2}, \nu_{3}\right)$ |
| 0.0 | $(0,0,0)$ | 0.0 | $(0,0,0)$ | 0.0 | $(0,0,0)$ |
| 1157.6 | $(0,1,0)$ | 1129.3 | $(0,1,0)$ | 1028.5 | $(0,1,0)$ |
| 2340.7 | $(0,2,0)$ | 2259.1 | $(0,2,0)$ | 1945.5 | $(0,2,0)$ |
| 2574.0 | $(1,0,0)$ | 2502.9 | $(1,0,0)$ | 2463.0 | $(1,0,0)$ |
| 2682.7 | $(0,0,1)$ | 2549.1 | $(0,0,1)$ | 2482.8 | $(0,0,1)$ |
| 3513.1 | $(0,3,0)$ | 3420.5 | $(0,3,0)$ | 2720.3 | $(0,3,0)$ |
| 3731.2 | $(1,1,0)$ | 3611.3 | $(0,1,1)$ | 3355.7 | $(0,4,0)$ |
| 3815.4 | $(0,1,1)$ | 3639.3 | $(1,1,0)$ | 3476.5 | $(0,1,1)$ |
| 4690.8 | $(0,4,0)$ | 4591.8 | $(0,4,0)$ | 3491.0 | $(1,1,0)$ |
| 4939.3 | $(1,2,0)$ | 4744.9 | $(0,2,1)$ | 4036.6 | $(0,5,0)$ |
| 4971.2 | $(0,2,1)$ | 4762.1 | $(1,2,0)$ | 4361.7 | $(0,2,1)$ |

${ }^{2}$ The symmetric stretching $\left(\nu_{1}\right)$, bending $\left(\nu_{2}\right)$, and antisymmetric stretching ( $\nu_{3}$ ) modes.
the rovibrational mixing of the $\widetilde{A}^{2} A_{1}$ and $\widetilde{X}^{2} B_{1}$ states can occur due to the Renner-Teller coupling, which is also a nonadiabatic process. However, in the present work, keeping the adiabaticity of the electronic states, we applied the Franck-Condon analysis to this system for understanding the Penning ionization mechanism. The $\widetilde{B}^{2} B_{2}$ state was found to cross near $130^{\circ}$ with the $\widetilde{C}^{2} A_{1}$ state, which has the S-H antibonding character of $\sigma_{\mathrm{s}}$ type. Nevertheless, we do not describe the latter state in detail since the purpose of this study is to describe the potential energy surfaces for the lowest three states of $\mathrm{H}_{2} \mathrm{~S}^{+}$.

Figure 4 shows the dependence of the electronic transition moment, $M$, for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{A}-\tilde{X})$ system on $\alpha$ at $\theta$ $=90^{\circ}$ and $r=1.9$ and $2.4 \AA$, which are where the equilib-


FIG. 5. Vibrational wave functions on the $R-r$ plane at $\theta=90^{\circ}$ for (a) the first state $(0,0,0)$ of $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$, (b) the fourth state $(1,0,0)$, (c) the 15th state $(0,6,0)$, and (d) the 27 th state $(1,5,0)$ of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$.
rium geometries are for the $\widetilde{X}$ and $\widetilde{A}$ states, respectively. The $M$ shows a peak at $\alpha=90^{\circ}-130^{\circ}$, which is around the equilibrium angles for both states. Although the $M$ increases with decreasing $r$ and deviating $\theta$ from $90^{\circ}$, the contribution from these areas to the pure bending transitions is expected to be small.

## B. Vibrational analysis

Table II summarizes the vibrational energies, $G$, of the lowest 11 states obtained for the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{X}^{2} B_{1}, \widetilde{A}^{2} A_{1}\right)$ states with their assignments. Figures 5 and 6 show the vibrational wave functions for these states on the $R-r$ plane at $\theta=90^{\circ}$. The nodal structures are clearly seen in these figures. The $\left(0,0, \nu_{3}^{\prime}=\right.$ odd $)$ state, which has a node on the plane with $\theta=90^{\circ}$, is not displayed.

Vibrational frequencies calculated for the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ states are compared with experimental data as well as other calculations in Table III. The bending progressions are found to be prominent in the preliminary analysis of the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ emission spectra produced by the Penning ionization of $\mathrm{H}_{2} \mathrm{~S}$ as described in Paper II. To examine the accuracy of the potential surfaces, especially concerning the bending mode, the vibrational frequencies for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ state obtained in this study are compared with the observed data ${ }^{26}$ in Table IV; the deviation from the observed data is evaluated to be within $11 \%$. Because the deviation from the observed energies does not seem to be accumulated in the range higher than $5000 \mathrm{~cm}^{-1}$, the accuracy of the vibrational energies for the $\widetilde{X}$ and $\widetilde{A}$ states of the ion is roughly estimated to be within $10 \%$ up to the $(0,10,0)$ state in this calculation.

For the $\mathrm{H}_{2} \mathrm{~S}(\tilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X})$ states, the vibrational quantum numbers have been assigned up to 56 and 77 levels, respectively. To elucidate the anharmonicity of the PES, a least-square analysis was applied to the vibrational frequencies of these levels using the well-known formula for three normal vibrations including anharmonicity constants; the vibrational frequency in reference to the vibrational ground state is given by ${ }^{27}$


FIG. 6. Vibrational wave functions on the $R-r$ plane at $\theta=90^{\circ}$ for (a) the tenth state $(0,5,0)$ of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$, and (b) the sixth state $(0,3,0)$, (c) the 23 rd state $(1,4,0)$, and (d) the 92 nd state $(0,11,0)$ of $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X})$.

$$
\begin{equation*}
G\left(\nu_{1}, \nu_{2}, \nu_{3}\right)=\sum_{i=1}^{3} \omega_{i}^{0} \nu_{i}+\sum_{i=1}^{3} \sum_{k \geqslant i}^{3} x_{i k}^{0} \nu_{i} \nu_{k} \tag{1}
\end{equation*}
$$

In contrast, such an analysis was very unsatisfactory for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ state; the standard deviation for the lowest 55 levels was $150 \mathrm{~cm}^{-1}$. We therefore introduced the third order term $y_{222}^{0} \nu_{2}^{3}$ in Eq. (1) since the $\nu_{2}$ energies show a large anharmonicity effect. The vibrational constants obtained for a best-fitted analysis are summarized in Table V. The anharmonicity constants for $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ are much larger than those
for $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X})$, indicating that the vibrational coupling is relatively large in the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ state.

The transition energy calculated for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ system is $18600 \mathrm{~cm}^{-1}$, which agrees well with the observed value of $18520 \mathrm{~cm}^{-1}$ and the calculated value of 18620 $\mathrm{cm}^{-1} .8,26$

## C. Franck-Condon factors

To evaluate the vibrational distributions of the $\mathrm{H}_{2} \mathrm{~S}^{+}\left(\widetilde{X}^{2} B_{1}, \widetilde{A}^{2} A_{1}\right)$ states produced by the Penning ionization of $\mathrm{H}_{2} \mathrm{~S}$, the FCFs were calculated for the $\left(\nu_{1}^{\prime \prime}=0, \nu_{2}^{\prime \prime}\right.$ $\left.=0, \nu_{3}^{\prime \prime}=0\right) \rightarrow\left(\nu_{1}^{\prime} \nu_{2}^{\prime} \nu_{3}^{\prime}\right)$ band of the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ transition. Table VI lists the results for the $\mathrm{H}_{2} \mathrm{~S}(\tilde{X})$ $\rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X})$ transition. In this transition the change in $r_{\mathrm{SH}}$ is only $0.02 \AA$, and the HSH angle does not change. Therefore, the main band is the transition to the vibrational ground state, and the FCF to the $(0,0,1)$ state is nearly zero since its wave function has a node on the $R-r$ plane at $\theta=90^{\circ}$. In contrast, the $\alpha$ is greatly enlarged with the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{A})$ transition, although the $r_{\text {SH }}$ length remains the same. Thus the bending mode ( $\nu_{2}^{\prime}$ ) is intensely enhanced in the ionization. Table VII summarizes the calculated results; the sum of the FCFs in the table is 0.93 . The $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ state, which is produced directly from $\mathrm{H}_{2} \mathrm{~S}$, may populate primarily in the ( $0, \nu_{2}^{\prime}=2-10,0$ ) states according to the Franck-Condon (FC) principle. In this calculation, the population maximum is at $\nu_{2}^{\prime}=6-7$, which is shifted higher than the peak around $\nu_{2}^{\prime}=4-5$ observed in the photoelectron spectrum of $\mathrm{H}_{2} \mathrm{~S}$, which is considered to be an FC type. ${ }^{26,29}$ This discrepancy is probably caused by the dependence of the electronic transition probability on the vibrational states, which is neglected in the FCFs. Therefore, Einstein's $B$ coefficients should be compared with the observed result. The maximum in Einstein's $B$ coefficients, which incorporate the dependence of

TABLE III. Calculated and observed vibrational frequencies for the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ states and the barrier to linearity in $\mathrm{cm}^{-1}$ units.

| State |  | This work ${ }^{\text {a }}$ | Theoretical | Observed |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ | $\nu_{1}$ | 2574 | ... | $2614.6^{\text {c }}$ |
|  | $\nu_{2}$ | 1158 | $\ldots$ | $1182.7^{\text {c }}$ |
|  | $\nu_{3}$ | 2683 | $\cdots$ | $2627.5^{\text {c }}$ |
| $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X})$ | $\nu_{1}$ | 2503 | $2710^{b}$ | $2380 \pm 50,{ }^{\mathrm{d}} 2516,{ }^{\mathrm{e}} 2485 \pm 40^{\mathrm{f}}$ |
|  | $\nu_{2}$ | 1129 | $1240,{ }^{\mathrm{b}} 1480^{\mathrm{j}}$ | $1165,^{\mathrm{g}} \sim 1000^{\mathrm{e}}$ |
|  | $\nu_{3}$ | 2549 | $2780^{\text {b }}$ | $\ldots$ |
| $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ | $\nu_{1}$ | 2463 | $2620^{\text {b }}$ | $2040 \pm 50^{\text {d }}$ |
|  | $\nu_{2}$ | 1029 | $1020,{ }^{\text {b }} 1150{ }^{\text {j }}$ | $\begin{aligned} & \sim 960,{ }^{\mathrm{g}} 940 \pm 50,{ }^{\mathrm{d}} 855,{ }^{\mathrm{e}} \\ & 910 \pm 10,{ }^{\mathrm{f}} 1088,{ }^{\mathrm{h}} 1080^{\mathrm{i}} \end{aligned}$ |
|  | $\nu_{3}$ | 2483 | $2580^{\text {b }}$ | $\cdots$ |
| $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X})$ barrier |  | 23100 | $23470^{\text {b }}$ | $23114^{\text {g }}$ |
| $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ barrier |  | 4600 | $4600^{\text {b }}$ | $4400^{8}$ |

${ }^{3}$ The difference between the first excited
state and the vibrational ground state.
${ }^{\mathrm{b}}$ Reference 8.
${ }^{\text {c }}$ Reference 26.
${ }^{\text {d Reference }} 29$.
${ }^{\mathrm{e}}$ Reference 30.
${ }^{\text {f }}$ Reference 32.
${ }^{\text {R }}$ Reference 28.
${ }^{h}$ Reference 33.
${ }^{\text {i }}$ Reference 34.
${ }^{\prime}$ Reference 6.

TABLE IV. Energy levels for the bending vibration of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ in $\mathrm{cm}^{-1}$ units.

| $\nu_{2}^{\prime}$ | Calculated $^{\mathrm{a}}$ | Observed $^{\mathrm{b}}$ | \% Difference |
| :---: | :---: | :---: | :---: |
| 0 | 0.0 | 0.0 | $\cdots$ |
| 1 | 1028.5 | $959.35^{*}$ | 7.2 |
| 2 | 1945.5 | $1893.05^{*}$ | 2.8 |
| 3 | 2720.3 | $2790.88^{*}$ | -2.5 |
| 4 | 3355.7 | 3666.23 | -8.5 |
| 5 | 4036.6 | 4539.97 | -11.1 |
| 6 | 4850.0 | 5445.66 | -10.9 |
| 7 | 5756.0 | 6403.76 | -10.1 |
| 8 | 6727.2 | $\cdots$ | $\cdots$ |
| 9 | 7745.9 | $\cdots$ | $\cdots$ |
| 10 | 8794.7 | $\cdots$ | $\cdots$ |

${ }^{\mathrm{a}}$ This work.
${ }^{\mathrm{b}}$ The figure with the asterisk $\left({ }^{*}\right)$ means the estimated value, Ref. 27.
the transition probability on the vibrational states for the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ ionization, is estimated to shift to lower $\nu_{2}^{\prime}$ than that of FCF since the transition moment is expected to be larger around the equilibrium geometry from the analogy of the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}-\widetilde{A})$ transition.

To analyze the vibrational populations of the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ emission spectra resulting in the collision of $\mathrm{He}^{*}\left(2^{3} S\right)$ with $\mathrm{H}_{2} \mathrm{~S}$, the FCFs were calculated for the $\left(\nu_{1}^{\prime}, \nu_{2}^{\prime}, \nu_{3}^{\prime}\right) \rightarrow\left(\nu_{1}^{\prime \prime}, \nu_{2}^{\prime \prime}, \nu_{3}^{\prime \prime}\right)$ band of the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\tilde{X})$ transition. The lowest 100 vibrational states of the $\widetilde{A}$ state and the lowest 200 vibrational states of the $\widetilde{X}$ state were included in the calculation. The $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ state produced from $\mathrm{H}_{2} \mathrm{~S}$ seems to be populated primarily in the $\left(0, \nu_{2}^{\prime}=2-10,0\right)$ states, assuming an FC-type ionization. In this context, the FCFs from the $\left(0, \nu_{2}^{\prime}=0-10,0\right)$ states are summarized in Table VIII. The $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ emission is expected to consist of pure bending progressions, and the contribution of the combination bands seems to be small. Although levels up to $\nu_{2}^{\prime}=14$ were observed in the photoelectron spectrum, ${ }^{32}$ no emissions from levels with $\nu_{2}^{\prime} \geqslant 7$ were observed because of the predissociation of $\mathrm{H}_{2} \mathrm{~S}^{+} .{ }^{26}$ Table IX lists Einstein's $A$ coefficients ${ }^{25}$ for the vibrational bands from the $\left(0, \nu_{2}^{\prime}\right.$ $=0-10,0)$ states. The peak in Einstein's $A$ coefficients from

TABLE V. Vibrational constants for $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ in $\mathrm{cm}^{-1}$ units.

|  | $\mathrm{H}_{2} \mathrm{~S}(\tilde{X})$ | $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{X})$ | $\mathrm{H}_{2} \mathrm{~S}^{+}(\tilde{A})$ |
| :---: | :---: | :---: | :---: |
| $n^{\mathrm{a}}$ | 56 | 73 | 55 |
| $\omega_{1}^{0}$ | 2598 | 2513 | 2583 |
| $\omega_{2}^{0}$ | 1179 | 1158 | 1102 |
| $\omega_{3}^{0}$ | 2658 | 2525 | 2533 |
| $x_{11}^{0}$ | -19 | -23 | -92 |
| $\chi_{22}^{0}$ | -1 | -1 | -87 |
| $\chi_{33}^{0}$ | -22 | -13 | -30 |
| $\chi_{12}^{0}$ | 5.5 | -11 | -38 |
| $\chi_{13}^{0}$ | -114 | -114 | -154 |
| $\chi_{23}^{0}$ | -20 | -22 | -44 |
| $y_{222}^{0}$ | $\cdots$ | $\cdots$ | 6 |
| $\sigma^{\mathrm{b}}$ | 50 | 44 | 63 |

[^2]TABLE VI. FCFs calculated for the $\left(\nu_{1}^{\prime \prime}=0, \nu_{2}^{\prime \prime}=0, \nu_{3}^{\prime \prime}=0\right) \rightarrow\left(\nu_{1}^{\prime}, \nu_{2}^{\prime}, \nu_{3}^{\prime}\right)$ band of the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X})$ transition.

| $\left(\nu_{1}^{\prime}, \nu_{2}^{\prime} \cdot \nu_{3}^{\prime}\right)$ | FCF |
| :---: | :---: |
| $(0,0,0)$ | 0.964 |
| $(0,1,0)$ | 0.008 |
| $(1,0,0)$ | 0.026 |
| $(0,0,1)$ | 0.000 |

each state is shifted lower than that for the corresponding FCFs because of both the dependence of the transition moment on the vibrational states and the third power of the transition energy.

Although Bruna et al. ${ }^{8}$ reported the FCFs for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ transition, they treated the calculation of the FCF as a one-dimensional model. Therefore, our data obtained by the three-dimensional calculation cannot be directly compared with their data; for example, the FCFs for the $(1,0,0)-\left(\nu_{2}^{\prime \prime}=0-2,0,0\right)$ bands are $0.0005,0.011$, and 0.0005 , respectively, against $0.143,0.959$, and 0.027 in Table 6 of Ref. 8 . We found that the FCFs from the $(1,0,0)$ state of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ are distributed widely among the combination states of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X})$. Thus, the one-dimensional treatment is insufficient for the vibrational states for $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ since the vibrational coupling is relatively large. The plot of FCFs for the $\nu_{2}^{\prime}\left(K^{\prime}=1\right)-\nu_{2}^{\prime \prime}=0\left(K^{\prime \prime}=0\right)$ progression in Fig. 6 of Ref. 8 may be comparable to the corresponding FCFs for the $\left(0, \nu_{2}^{\prime}, 0\right)-(0,0,0)$ transition in Table VIII. The data in this study have a maximum at $\nu_{2}^{\prime}=6-7$ against a maximum at $\nu_{2}^{\prime}=5-6$ in Ref. 8. The difference may originate in the three-dimensional treatment of FCF against the onedimensional model of the vibrational states rather than the PES.

## IV. CONCLUSION

The potential energy surfaces of $\mathrm{H}_{2} \mathrm{~S}(\tilde{X})$ and $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ were obtained from the MCSCF/MRCI method in this study. The vibrational energies were calculated for these electronic states, and the vibrational states were as-

TABLE VII. FCFs calculated for the $(0,0,0) \rightarrow\left(\nu_{1}^{\prime}, \nu_{2}^{\prime}, 0\right)$ band of the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ transition.

| $\nu_{2}^{\prime}$ | $\left(0, \nu_{2}^{\prime}, 0\right)$ | $\left(1, \nu_{2}^{\prime}, 0\right)$ | $\left(2, \nu_{2}^{\prime}, 0\right)$ |
| :---: | :---: | :---: | :---: |
| 0 | 0.006 | 0.001 | 0.000 |
| 1 | 0.025 | 0.004 | 0.008 |
| 2 | 0.049 | 0.007 | 0.000 |
| 3 | 0.064 | 0.008 | 0.011 |
| 4 | 0.073 | 0.004 | $\cdots$ |
| 5 | 0.106 | 0.014 | $\cdots$ |
| 6 | 0.129 | 0.008 | $\cdots$ |
| 7 | 0.126 | 0.020 | $\cdots$ |
| 8 | 0.106 | 0.023 | $\cdots$ |
| 9 | 0.075 | 0.022 | $\cdots$ |
| 10 | 0.041 | $\cdots$ | $\cdots$ |

TABLE VIII. FCFs calculated for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\tilde{X})$ transitions and related vibrational energies $G$.

| $\widetilde{X}$ state | $\widetilde{A}$ state | $(0,0,0)$ | $(0,1,0)$ | $(0,2,0)$ | $(0,3,0)$ | $(0,4,0)$ | $(0,5,0)$ | $(0,6,0)$ | $(0,7,0)$ | $(0,8,0)$ | $(0,9,0)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\left(G / \mathrm{cm}^{-1}\right)$ | 0 | 1029 | 1946 | 2720 | 3356 | 4037 | 4850 | 5756 | 6727 | 7746 |
| $(0,0,0)$ | 0 | 0.010 | 0.038 | 0.069 | 0.083 | 0.091 | 0.125 | 0.145 | 0.135 | 0.108 | 0.070 |
| $(0,1,0)$ | 1129 | 0.051 | 0.118 | 0.125 | 0.084 | 0.047 | 0.021 | 0.000 | 0.017 | 0.070 | 0.113 |
| $(0,2,0)$ | 2259 | 0.113 | 0.142 | 0.061 | 0.006 | 0.002 | 0.030 | 0.073 | 0.071 | 0.025 | 0.001 |
| $(0,3,0)$ | 3421 | 0.162 | 0.081 | 0.000 | 0.024 | 0.051 | 0.063 | 0.025 | 0.001 | 0.049 | 0.078 |
| $(0,4,0)$ | 4592 | 0.162 | 0.012 | 0.031 | 0.057 | 0.033 | 0.004 | 0.017 | 0.064 | 0.042 | 0.000 |
| $(0,5,0)$ | 5767 | 0.125 | 0.003 | 0.061 | 0.024 | 0.000 | 0.021 | 0.052 | 0.013 | 0.011 | 0.063 |
| $(0,6,0)$ | 6930 | 0.081 | 0.029 | 0.041 | $\cdots .000$ | 0.015 | 0.036 | 0.009 | 0.015 | 0.048 | 0.008 |
| $(0,7,0)$ | 8073 | 0.049 | 0.050 | 0.012 | 0.010 | 0.025 | 0.012 | 0.005 | 0.038 | 0.006 | 0.019 |
| $(0,8,0)$ | 9202 | 0.031 | 0.063 | 0.000 | 0.025 | 0.016 | 0.000 | 0.027 | 0.012 | 0.011 | 0.029 |
| $(0,9,0)$ | 10327 | 0.023 | 0.078 | 0.008 | 0.035 | 0.004 | 0.014 | 0.029 | 0.001 | 0.037 | 0.002 |
| $(0,10,0)$ | 11425 | 0.015 | 0.081 | 0.038 | 0.026 | 0.002 | 0.037 | 0.008 | 0.027 | 0.020 | 0.016 |
| $(0,11,0)$ | 12485 | 0.008 | 0.063 | 0.068 | 0.006 | 0.019 | 0.033 | 0.002 | 0.038 | 0.000 | 0.040 |
| $(0,12,0)$ | 13525 | 0.004 | 0.043 | 0.085 | 0.000 | 0.036 | 0.010 | 0.026 | 0.014 | 0.025 | 0.014 |
| $(1,0,0)$ | 2503 | 0.000 | 0.000 | 0.001 | 0.002 | 0.003 | 0.005 | 0.008 | 0.008 | 0.010 | 0.000 |
| $(1,2,0)$ | 4762 | 0.020 | 0.004 | 0.001 | 0.004 | 0.003 | 0.002 | 0.000 | 0.002 | 0.001 | 0.000 |
| $(1,3,0)$ | 5940 | 0.032 | 0.000 | 0.012 | 0.008 | 0.001 | 0.002 | 0.009 | 0.010 | 0.000 | 0.004 |
| $(1,4,0)$ | 7091 | 0.030 | 0.009 | 0.015 | 0.001 | 0.004 | 0.012 | 0.007 | 0.000 | 0.009 | 0.002 |
| $(1,5,0)$ | 8232 | 0.027 | 0.028 | 0.008 | 0.004 | 0.014 | 0.009 | 0.000 | 0.010 | 0.005 | 0.007 |
| $(1,6,0)$ | 9338 | 0.018 | 0.039 | 0.000 | 0.015 | 0.012 | 0.000 | 0.012 | 0.010 | 0.002 | 0.020 |
| , |  |  |  |  |  |  |  |  |  | 0.000 |  |

signed. The accuracy of the vibrational energies for $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X}, \widetilde{A})$ is roughly estimated to be $10 \%$ up to 8000 $\mathrm{cm}^{-1}$. We believe that this accuracy is adequate for calculating the FCFs for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\widetilde{X})$ transition. The FCFs for the $\mathrm{H}_{2} \mathrm{~S}(\widetilde{X}) \rightarrow \mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ ionization show that the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ state primarily populates in the $\left(0, \nu_{2}^{\prime}=2-10,0\right)$ state with a maximum around $\nu_{2}^{\prime}=6-7$. This feature is, however, shifted higher than that of the photoelectron spectra of $\mathrm{H}_{2} \mathrm{~S}$, which show a peak at $\nu_{2}^{\prime}=4-5 .{ }^{26,32}$ For a more accurate comparison with the observed data, we need to obtain Einstein's $B$
coefficients, which incorporate the dependence of the transition probability on the vibrational states. Even if the pure bending state of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ is primarily produced, some combination states may be populated through the vibrational coupling. We found that the FCFs calculated for some combination states near the $\left(0, \nu_{2}^{\prime}=2-10,0\right)$ states of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ are dispersed among several vibrational states of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{X})$. Therefore, even if any emissions from combination states do occur, they would be hidden by intense bending progressions, which is consistent with there being no emissions as-

TABLE IX. Einstein's $A$ coefficients calculated for the $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A}-\tilde{X})$ transitions.

| $\widetilde{X}$ state | $\widetilde{A}$ state |  |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | $(0,0,0)$ | $(0,1,0)$ | $(0,2,0)$ | $(0,3,0)$ | $(0,4,0)$ | $(0,5,0)$ | $(0,6,0)$ | $(0,7,0)$ | $(0,8,0)$ | $(0,9,0)$ | $(0,10,0)$ |
| $(0,0,0)$ | 86 | 316 | 579 | 711 | 784 | 1083 | 1266 | 1185 | 946 | 612 | 296 |
| $(0,1,0)$ | 385 | 899 | 969 | 655 | 367 | 166 | 2 | 138 | 558 | 884 | 905 |
| $(0,2,0)$ | 770 | 989 | 428 | 44 | 17 | 219 | 542 | 539 | 196 | 3 | 313 |
| $(0,3,0)$ | 1005 | 521 | 4 | 154 | 331 | 412 | 167 | 7 | 330 | 542 | 222 |
| $(0,4,0)$ | 917 | 81 | 166 | 329 | 202 | 26 | 93 | 362 | 246 | 1 | 302 |
| $(0,5,0)$ | 644 | 10 | 306 | 136 | 3 | 94 | 265 | 73 | 51 | 324 | 149 |
| $(0,6,0)$ | 370 | 109 | 198 | 3 | 56 | 162 | 51 | 57 | 215 | 41 | 96 |
| $(0,7,0)$ | 193 | 177 | 60 | 29 | 97 | 56 | 14 | 147 | 29 | 66 | 156 |
| $(0,8,0)$ | 101 | 194 | 2 | 79 | 62 | 0 | 87 | 50 | 31 | 105 | 0 |
| $(0,9,0)$ | 56 | 193 | 16 | 95 | 14 | 34 | 92 | 1 | 112 | 11 | 100 |
| $(0,10,0)$ | 27 | 154 | 71 | 60 | 2 | 83 | 24 | 61 | 59 | 37 | 88 |
| $(0,11,0)$ | 10 | 89 | 100 | 13 | 29 | 62 | 3 | 77 | 0 | 86 | 0 |
| $(0,12,0)$ | 3 | 44 | 93 | 0 | 45 | 17 | 34 | 26 | 35 | 27 | 43 |
| $(1,0,0)$ | 0 | 0 | 1 | 4 | 8 | 12 | 19 | 24 | 3 | 13 | 32 |
| $(1,2,0)$ | 74 | 8 | 11 | 28 | 14 | 4 | 5 | 33 | 13 | 0 | 11 |
| $(1,3,0)$ | 113 | 3 | 60 | 30 | 0 | 18 | 60 | 50 | 4 | 44 | 4 |
| $(1,4,0)$ | 96 | 40 | 59 | 1 | 21 | 57 | 27 | 0 | 56 | 8 | 26 |
| $(1,5,0)$ | 73 | 93 | 23 | 17 | 55 | 32 | 3 | 45 | 20 | 39 | 47 |
| $(1,6,0)$ | 39 | 105 | 0 | 48 | 36 | 0 | 46 | 33 | 11 | 79 | 0 |

signed from combination state. ${ }^{28}$ These findings indicate that the vibrational distribution of $\mathrm{H}_{2} \mathrm{~S}^{+}(\widetilde{A})$ obtained from the analysis of emission spectra is not deviated by combination bands.

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[^1]:     the energy difference from the $\mathrm{H}_{2} \mathrm{~S}\left(\widetilde{X}^{1} A_{1}\right)$ state.
    ${ }^{\mathrm{b}}$ Reference 8.
    ${ }^{\text {c }}$ Reference 27.
    ${ }^{\text {d }}$ Reference 26.
    ${ }^{\text {e }}$ Reference 28.
    ${ }^{\mathrm{f}}$ Adiabatic ionization potential, Ref. 29.
    ${ }^{8}$ Reference 30.
    ${ }^{\text {h }}$ Reference 31.
    ${ }^{\text {i}}$ Reference 32.

[^2]:    ${ }^{2}$ The number of vibrational levels included in the analysis.
    ${ }^{\mathrm{b}}$ The standard deviation for vibrational frequencies.

